

AIM 08 Performance measurement

AIM 08.2 Single-factor risk-adjusted performance

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Risk-adjusted performance

□ Context:

- Risk-adjusted performance evaluation is critical in investment management.
 - Can active portfolio managers outperform benchmarks after accounting for risk and management fees?

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Risk-adjusted performance

□ Purpose:

- Discuss four traditional portfolio performance measures are based on CAPM.
 - Two are based on CML.
 - Sharpe ratio
 - M-squared
 - Two are based on SML.
 - Treynor ratio
 - Jensen's alpha

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Risk-adjusted performance

□ Purpose:

- Discuss two other measures are ad hoc, albeit intuitive.
 - One is based on excess return regression.
 - Treynor/Black appraisal ratio
 - One is based on ad hoc measure of risk.
 - Sortino ratio
- Introduce concept called portable alpha.
 - Direct by-product of Jensen's alpha.

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CAPM assumptions

- Markowitz (*JF* 1952) assumed n risky assets.
- Tobin (*REST* 1958) showed link between diminishing positive marginal utility of wealth and risk averse indifference curves.
- Sharpe (*JF* 1964) added risk-free cash equivalents to set of securities in capital market.
 - Assumed individuals can borrow or lend at risk-free interest rate, r .

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CAPM results/predictions

- CAPM has three main results.

- 1. Capital market line (*)

$$E_P = r + (E_M - r) \left(\frac{\sigma_P}{\sigma_M} \right)$$

- 2. Composition of market portfolio

$$X_i = V_i / V_M$$

- 3. Security market line (*)

$$E_i = r + (E_M - r) \beta_i$$

(*) denotes two CAPM results that are foundation of traditional performance measures.

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Total risk measures

□ Two measures are based on total risk (CML).

Expectations	Realizations
<i>Sharpe ratio</i>	
$E(SR) \equiv \frac{E_S - r}{\sigma_S} = \frac{E_M - r}{\sigma_M}$	$SR \equiv \frac{\bar{R}_S - \bar{R}_F}{\hat{\sigma}_S} = \frac{\bar{R}_M - \bar{R}_F}{\hat{\sigma}_M}$
<i>M-squared</i>	
$E(M^2) \equiv E_S - r - \left(\frac{E_M - r}{\sigma_M} \right) \sigma_S = 0$	$M^2 \equiv \bar{R}_S - \bar{R}_F - \left(\frac{\bar{R}_M - \bar{R}_F}{\hat{\sigma}_M} \right) \hat{\sigma}_S$

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Systematic risk measures

□ Two measures are based on beta (SML).

Expectations	Realizations
<i>Treynor ratio</i>	
$E(TR) \equiv \frac{E_S - r}{\beta_S} = E_M - r$	$TR \equiv \frac{\bar{R}_S - \bar{R}_F}{\hat{\beta}_S} = \bar{R}_M - \bar{R}_F$
<i>Jensen's alpha</i>	
$E(\alpha) \equiv E_S - r - (E_M - r) \beta_S = 0$	$\hat{\alpha} \equiv \bar{R}_S - \bar{R}_F - (\bar{R}_M - \bar{R}_F) \hat{\beta}_S$

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Appraisal ratio

- Measures risk-adjusted reward from active management.
 - Jensen's alpha divided by residual risk (i.e., standard error of regression estimate).

$$AR = \frac{\hat{\alpha}}{\hat{\sigma}_{\varepsilon}}$$

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Sortino ratio

- Measures Sharpe ratio using down-side risk.
 - CAPM assumes individuals are equally unhappy about large positive returns as large negative returns.
 - Some argue that only latter matters.
 - Define risk as:

$$\sigma_{S,semi-deviation} = \sqrt{\frac{\sum_{t=1}^T \min(R_{S,t} - R_{F,t}, 0)^2}{T}}$$

$$\text{Sortino ratio} = \frac{\bar{R}_S - \bar{R}_F}{\hat{\sigma}_{S,semi-deviation}}$$

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Illustration

IYW

iShares U.S. Technology ETF

Fact Sheet as of 12/31/2022

KEY FACTS

Fund Launch Date05/15/2000

Expense Ratio0.39%

BenchmarkRussell 1000 Technology

RIC 22 5/45 Capped Index

30 Day SEC Yield0.56%

Number of Holdings140

Net Assets\$7,827,660,617

TickerIYW

CUSIP464287721

ExchangeNYSE Arca

TOP HOLDINGS (%)

APPLE INC17.79

MICROSOFT CORP16.51

ALPHABET INC CLASS A5.13

ALPHABET INC CLASS C4.58

NVIDIA CORP4.22

META PLATFORMS INC CLASS A3.65

BROADCOM INC3.22

ADOBE INC2.36

TEXAS INSTRUMENT INC2.26

SALESFORCE INC1.93

61.65

Holdings are subject to change.

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Data

Download 3 years of daily total return index data from Bloomberg.

Eliminated non-US trading days.

Support file: IYW analysis.xlsx

IYW: iShares Technology ETF

VOO: Vanguard S&P 500 ETF

SPX: S&P 500 index

VTI: Vanguard Total Stock Market ETF

CRSPTMT: CRSP Total market index

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Analysis

❑ Compute summary statistics.

Return summary statistics						
Description	IYW	VOO	SPX	VTI	CRSPTMT	EFFR
<i>n</i>	756	756	756	756	756	756
Mean (daily)	0.00035	0.00029	0.00029	0.00027	0.00027	0.00003
StDev (daily)	0.02080	0.01608	0.01611	0.01627	0.01645	0.00006
Skewness	-0.43874	-0.73061	-0.74355	-0.74483	-0.83969	3.44605
Autocorrelation	-0.18844	-0.20893	-0.21618	-0.18298	-0.19878	0.57987
Minimum	-0.14646	-0.12487	-0.12761	-0.12082	-0.13128	0.00000
Median	0.00138	0.00094	0.00094	0.00088	0.00085	0.00000
Maximum	0.10701	0.09109	0.08977	0.09066	0.09036	0.00048
Mean (annual)	8.79%	7.34%	7.36%	6.74%	6.76%	0.72%
StDev (annual)	33.02%	25.53%	25.57%	25.83%	26.12%	0.09%
CAGR	9.19%	7.62%	7.64%	6.97%	6.99%	0.72%
HPR	30.17%	24.63%	24.72%	22.42%	22.46%	2.18%

Tech ETF had higher return than S&P 500 ETF
but at greater risk.

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Analysis

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HPR	30.17%	24.63%	24.72%	22.42%	22.46%	2.18%

ETFs had lower returns than benchmark.

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Analysis

❑ Compute correlations.

	IYW	VOO	SPX	VTI	CRSPTMT	EEFR
IYW	1	0.925	0.927	0.926	0.927	-0.055
VOO	0.925	1	0.999	0.996	0.996	-0.045
SPX	0.927	0.999	1	0.996	0.997	-0.046
VTI	0.926	0.996	0.996	1	0.999	-0.048
CRSPTMT	0.927	0.996	0.997	0.999	1	-0.049
EEFR	-0.055	-0.045	-0.046	-0.048	-0.049	1

Cash equivalents return uncorrelated with stock market.

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Analysis

❑ Compute correlations.

	IYW	VOO	SPX	VTI	CRSPTMT	EEFR
IYW	1	0.925	0.927	0.926	0.927	-0.055
VOO	0.925	1	0.999	0.996	0.996	-0.045
SPX	0.927	0.999	1	0.996	0.997	-0.046
VTI	0.926	0.996	0.996	1	0.999	-0.048
CRSPTMT	0.927	0.996	0.997	0.999	1	-0.049
EEFR	-0.055	-0.045	-0.046	-0.048	-0.049	1

Stock market indexes are highly correlated.

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Analysis

❑ Compute correlations.

Correlation matrix						
	IYW	VOO	SPX	VTI	CRSPTMT	EEFR
IYW	1	0.925	0.927	0.926	0.927	-0.055
VOO	0.925	1	0.999	0.996	0.996	-0.045
SPX	0.927	0.999	1	0.996	0.997	-0.046
VTI	0.926	0.996	0.996	1	0.999	-0.048
CRSPTMT	0.927	0.996	0.997	0.999	1	-0.049
EEFR	-0.055	-0.045	-0.046	-0.048	-0.049	1

Tech ETF is less than perfectly correlated because it is not as well diversified.

- Tactical allocation or market timing strategy.
 - Your decision; not active manager's.
 - IYW is passive portfolio of tech stocks.

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Analysis

❑ Compute IYW performance measures.

Risk-adjusted performance				
Description	VOO	SPX	VTI	CRSPTMT
<i>n</i>	756	756	756	756
Sharpe ratio - portfolio	0.0154	0.0154	0.0154	0.0154
Sharpe ratio - market	0.0163	0.0164	0.0147	0.0146
M-squared	0.0000	0.0000	0.0000	0.0000
Treynor ratio - portfolio	0.0003	0.0003	0.0003	0.0003
Treynor ratio - market	0.0003	0.0003	0.0002	0.0002
Jensen's alpha	0.0000	0.0000	0.0000	0.0000
Appraisal ratio	0.0007	0.0006	0.0047	0.0051
Sortino ratio - portfolio	0.0211	0.0211	0.0211	0.0211
Sortino ratio - market	0.0221	0.0222	0.0198	0.0196
M-squared - CAGR	-0.49%	-0.51%	0.37%	0.44%
Jensen's alpha - CAGR	0.15%	0.12%	0.94%	1.00%

When benchmarked to tradable S&P 500 (VOO ETF) or S&P 500 benchmark, poor risk-adjusted performance.

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Analysis

- Compute IYW performance measures.

Risk-adjusted performance				
Description	VOO	SPX	VTI	CRSPTMT
<i>n</i>	756	756	756	756
Sharpe ratio - portfolio	0.0154	0.0154	0.0154	0.0154
Sharpe ratio - market	0.0163	0.0164	0.0147	0.0146
M-squared	0.0000	0.0000	0.0000	0.0000
Treynor ratio - portfolio	0.0003	0.0003	0.0003	0.0003
Treynor ratio - market	0.0003	0.0003	0.0002	0.0002
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Sortino ratio - portfolio	0.0211	0.0211	0.0211	0.0211
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M-squared - CAGR	-0.49%	-0.51%	0.37%	0.44%
Jensen's alpha - CAGR	0.15%	0.12%	0.94%	1.00%

When benchmarked to tradable total market index (VTI ETF) or CRSPTMT benchmark, good risk-adjusted performance.

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Analysis

- Compute IYW performance measures.

Risk-adjusted performance				
Description	VOO	SPX	VTI	CRSPTMT
<i>n</i>	756	756	756	756
Sharpe ratio - portfolio	0.0154	0.0154	0.0154	0.0154
Sharpe ratio - market	0.0163	0.0164	0.0147	0.0146
M-squared	0.0000	0.0000	0.0000	0.0000
Treynor ratio - portfolio	0.0003	0.0003	0.0003	0.0003
Treynor ratio - market	0.0003	0.0003	0.0002	0.0002
Jensen's alpha	0.0000	0.0000	0.0000	0.0000
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Sortino ratio - portfolio	0.0211	0.0211	0.0211	0.0211
Sortino ratio - market	0.0221	0.0222	0.0198	0.0196
M-squared - CAGR	-0.49%	-0.51%	0.37%	0.44%
Jensen's alpha - CAGR	0.15%	0.12%	0.94%	1.00%

Ratios like Sharpe ratio and Treynor have little economic appeal.

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Analysis

❑ Compute IYW performance measures.

Risk-adjusted performance				
Description	VOO	SPX	VTI	CRSPTMT
<i>n</i>	756	756	756	756
Sharpe ratio - portfolio	0.0154	0.0154	0.0154	0.0154
Sharpe ratio - market	0.0163	0.0164	0.0147	0.0146
M-squared	0.0000	0.0000	0.0000	0.0000
Treynor ratio - portfolio	0.0003	0.0003	0.0003	0.0003
Treynor ratio - market	0.0003	0.0003	0.0002	0.0002
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Appraisal ratio	0.0007	0.0006	0.0047	0.0051
Sortino ratio - portfolio	0.0211	0.0211	0.0211	0.0211
Sortino ratio - market	0.0221	0.0222	0.0198	0.0196
M-squared - CAGR	-0.49%	-0.51%	0.37%	0.44%
Jensen's alpha - CAGR	0.15%	0.12%	0.94%	1.00%

Investors/managers want outperformance expressed in annualized return percentage.

$$CAGR = e^{daily\ outperformance \times 252} - 1$$

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Attributes of benchmark

❑ Must be all-inclusive.

■ Should not use S&P 500.

■ Leaves VTI and CRSPTMT.

❑ Must be investable (or tradable).

■ Leaves VTI.

❑ Must account for costs.

■ VTI returns are after management fees (i.e., expense ratio).

❑ Must have liquid market.

■ Bid/ask spread is \$0.01 (or less).

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Isolate alpha

- Suppose you want gains from tech stocks, not gains or losses from overall market.
 - Can you isolate returns from your tactical decision?

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Isolate alpha

- Measure relative market risk, β , using VTI.
- Supporting sheet: Portable alpha
 - Beta is 1.18355.

Excess return regression - VTI	
Benchmark index	IYW
n	756
α	0.00004
$s(\alpha)$	0.00029
β	1.18355
$s(\beta)$	0.01759
R-squared	0.8573
Adj. R-squared	0.8571
Std error of estimate	0.00786
t -ratio ($H_0: \alpha=0$)	0.13
t -ratio ($H_0: \beta=1$)	10.44

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Isolate alpha

- Create hedged portfolio by short selling VTI.
 - Call it “Alpha portfolio.”
 - Amount to short sell is 1.18355 VTI return.
 - Invest cash generated in cash equivalents.
 - Support sheet: Portable alpha

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Isolate alpha

- Consider short selling market ETF against your tactical allocation to IYW.
 - Excess return regress produces estimates of alpha and beta.
- By OLS regression assumptions,

$$R_{S,t} - R_{F,t} = \alpha_S + \beta_S (R_{M,t} - R_{F,t}) + \varepsilon_{S,t}$$

$$\bar{R}_S = \hat{\alpha} + \bar{R}_F + \hat{\beta}_S (\bar{R}_M - \bar{R}_F)$$

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Portable alpha

- For active funds, alpha measures manager's skill.
 - Skill can be isolated by creating hedged portfolio:
 - Short sell passively managed market index ETF.
 - Effectively turns portfolio into investment whose expected excess return equals alpha with no investment.
 - Sell futures on market index.
 - Effectively turns portfolio into investment whose expected excess return equals alpha plus risk-free rate earned on original investment amount.

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Portable alpha benchmarks

- Portable alpha requires actively-traded market price risk factor.
 - For stocks, use:
 - All-inclusive, inexpensive, total market index ETP like VTI.
 - Futures contract written on broad-based index like S&P 500 futures (CME).
 - For bonds, use:
 - All-inclusive, inexpensive, total market index ETP like BND.
 - Futures contract written on broad-based index like Treasury bond futures (CBT).

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BOND

❑ Illustration: Short sell BND against long position in BOND to generate daily alpha return.

Regressions on BND		
	BOND	Alpha
n	2,701	2,701
α	0.000049	0.000049
$s(\alpha)$	0.000028	0.000028
β	0.809242	0.000000
$s(\beta)$	0.009103	0.009103
R-squared	0.7454	0.0000
Adj. R-squared	0.7453	-0.0004
Std error of estimate	0.00146	0.00146

Run regression of excess return of BOND on excess return of BND.

For every dollar invested in BOND, sell 0.809242 dollars in BND.

$\alpha_t = XR_{BOND,t} - 0.781603 \times XR_{BND,t}$

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BOND

❑ Illustration: Short sell BND against long position in BOND to generate daily alpha return.

Regressions on BND		
	BOND	Alpha
n	2,701	2,701
α	0.000049	0.000049
$s(\alpha)$	0.000028	0.000028
β	0.809242	0.000000
$s(\beta)$	0.009103	0.009103
R-squared	0.7454	0.0000
Adj. R-squared	0.7453	-0.0004
Std error of estimate	0.00146	0.00146

No long-term interest rate risk (i.e., market risk) remains.

Outperformance does.

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Lesson summary

- Active fund return is attributable to:
 - Market risk exposures: Betas (not just stock market)
 - Investment skills: Portable alpha
- Do not need manager to create market risk exposures.
 - Can create cheaply using futures or passive ETPs.

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Lesson summary

- Described four traditional risk-adjusted performance measures.
 - Two are based on total volatility.
 - Sharpe ratio
 - M-squared
 - Two are based on beta.
 - Treynor ratio
 - Jensen alpha

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Lesson summary

- Discussed two other measures are ad hoc, albeit intuitive.
 - One is based on excess return regression.
 - Treynor/Black appraisal ratio
 - One is based on ad hoc measure of risk.
 - Sortino ratio
- Introduced concept called portable alpha.
 - Direct by-product of Jensen's alpha.
 - Can transport alpha (i.e., outperformance) across asset categories.

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Lesson summary

- Understand source of portable alpha.
 - Why are prices incorrect and what forces them to correct?

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